

MULTILEVEL INVERTER SOLUTION FOR PRESENT INVERTER IN LOCAL TRAINS IN MUMBAI

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ABSTRACT

In this paper presents literature survey for the implementation multilevel inverter in Mumbai Local Trains. Also present latest inverter system implemented in the local trains. This will also give the information about the Total Harmonic Distortion in the traction system. Initially Total Harmonic Distortion and losses due to that will be considered for the present system inverter and various topologies are studied with their advantages and disadvantages.

KEYWORDS: Multilevel Inverter, Total Harmonic Distortion, Electric Traction

INTRODUCTION

Due to the improvement of fast-switching Power-electronic inverters are becoming popular for various industrial drives applications. In recent years also high-power and medium-voltage drive applications have been installed. To overcome the limited semiconductor voltage and current ratings, some kind of series and/or parallel connection will be necessary. Due to their ability to synthesize waveforms with a better harmonic spectrum and attain higher voltages, multi-level inverters are receiving increasing attention in the past few years. The multilevel inverter was introduced as a solution to increase the converter operating voltage above the voltage limits of classical semiconductors. The multilevel voltage source inverter is recently applied in many industrial applications such as ac power supplies, static VAR compensators, drive systems, etc. One of the significant advantages of multilevel configuration is the harmonic reduction in the output waveform without increasing switching frequency or decreasing the inverter power output. The output voltage waveform of a multilevel inverter is composed of the number of levels of voltages, typically obtained from capacitor voltage sources. The so-called multilevel starts from three levels. As the number of levels reach infinity, the output THD (Total Harmonic Distortion) approaches zero. The number of the achievable voltage levels, however, is limited by voltage unbalance problems, voltage clamping requirement, circuit layout, and packaging constraints. Multilevel inverters synthesizing a large number of levels have a lot of merits such as improved output waveform, a smaller filter size, a lower EMI (Electro Magnetic Interference), and other advantages. The principle advantage of using multilevel inverters is the low harmonic distortion obtained due to the multiple voltage levels at the output and reduced stresses on the switching devices used. To avoid these problems several solutions have been developed. One of them is introducing additional output filter. This method is questionable for high current drives because of voltage drops on filter passive components and additional losses. The concept of multilevel power conversion came to has article since from 1975 and term multilevel began with the three-level converter first time by Nabae. Subsequently, several multilevel converter topologies have been developed and proposed. But however, basic concept of multilevel converter achieving higher power rating by using a series of semiconductor switches with several low voltage dc sources to perform the power conversion by synthesizing a staircase voltage waveform. Capacitors, batteries, and renewable energy systems used as the multiple dc voltage sources.

The commutation of the power switches aggregate these multiple dc sources in order to achieve high voltage at the output; however, voltage rating of the power semiconductor switches depends on rating of dc bus to which they are connected. The attractive benefits of multilevel converters when compared with conventional 2-level converter are briefly summarized as follows:

- **Quality of Output Voltage:** Multilevel converters generate the output voltages with very low distortion, additionally reduce the dv/dt stresses; therefore electromagnetic compatibility (EMC) problems significantly minimized.
- **Quality of Input Current:** Multilevel converters draw input current with very low distortion.
- **Quality of Switching Frequency:** Multilevel converters can modulate with fundamental and also higher switching frequency PWM. By lower switching frequency provides lower switching loss and higher efficiency.

Quality of Reducing Common Mode Voltage

Multilevel converters produce smaller common mode (CM) voltages; therefore, the stress in the bearings of a motor can be lowered. Further common-mode components could eliminate by using advanced PWM strategies. Even though with all above merits, multilevel converters do possess some drawbacks in particular with greater number of power switches. Lower voltage rated switches can utilized in a multilevel converter, but each switch requires related gate driver circuit. Hence, the overall system becomes expensive with complex control. In next section, most addressed available multilevel converter structures are discussed relating to survey of optimal configuration solution.

LITERATURES SURVEY REGARDING TOTAL HARMONIC DISTORTION, IMPLEMENTATION OF MULTILEVEL INVERTERS IN TRACTION

Reduction of Harmonics

N. Gunavardhin, M. Chandrasekaran, A. D. Thirumoorthy [1] have done the study on two railway traction sub-stations. One is Salem 110KV Railway traction where 2400 KVAR rated capacitor bank alone is installed and another is Bommidi 110 KV Railway traction where IGBT based Dynamic Reactive Power Compensation (DRPC) with 1800 KVAR is connected along with fixed 2400KVAR capacitor bank. The harmonics due to load currents are measured and compared in both the sub-stations based on IEEE Standards 519-1992. Shu-Guang Sun, Jing-Qin Wang, Shun-Quan Shi[2] have done the work on detection of harmonics and reactive currents of active power filter (APF) The former is the detection method based on the character of triangle function and some improvements are done; The latter is the detection method based on the theory of adaptive linear neural network. Yu Han, Cui Zhengpai, Li Sheng, Liu Qihui, Long Yunbo, Zhang Jianhua [3] presents an approach to the detection of harmonics and reactive currents in single-phase circuit according to the orthogonal characteristic of sine function. The method is simple and practical, which cannot only detect the current component in the distorted current but can also obtain the sum of the active and reactive current. H. J. Chuang, C. S. Chen, C. H. Lin, and H. M. Shiao [4] investigate the stochastic harmonic distortion of an mass rapid transit (MRT) system by considering the dynamic load behavior of train sets. The mathematical model of 12-pulse uncontrolled rectifiers without interphase transformers has been used in the harmonic load flow analysis to solve the power demand and harmonic current injection for each time snapshot. I. Zamora¹, P. Eguia², A. J. Mazón, E. Torres, K. J. Sagastabeitia [5] the simulation of an active filter for the reduction of the current harmonic distortion of an underground traction system is presented. Karel HLAVA, Radovan DOLEČEK [6] deals with the wave distortion analysis of the contact system line voltage at the operation of electric motive power with diode traction converters. The ascertained harmonic values are important for the prepared european standards and guidelines about interoperability not only from the point of view of the

energy measurements on board trains working conditions, but also from the point of view to insure the regenerative braking safety of new AC motive power. Adrian David Cheok and Shoichi Kawamoto, Takeo Matsumoto, and Hideo Obi [7] work on advanced control techniques lead to a unity power factor seen by the ac supply as well as minimizing the line harmonics, power loss, motor torque ripple, and audible noise.

By using advanced ac inverter drive systems the recently developed high speed train offers high level performance, efficiency, and passenger comfort. The described system is implemented in the latest “Bullet” or Shinkansen train sets operating in eastern Japan between Tokyo and Nagano. Vasanthi V, and Ashok Sinvestigate [8] the harmonics of Electric Traction system in Indian railways by taking measurements at 110/25kV traction substations. This also calculates the total harmonic distortion of current and voltage harmonics in the feeder of the traction substation. Urmila Bandaru, Subba D Rayudu [21] presents a comparative study of orientation of higher ordered harmonics with increase in switching frequency around the frequency modulation index of nine level diode clamped inverter for different Switching frequency Multicarrier Pulse width Modulation. Shouji Onda*, Katsumi Maekawa [22] presents a paper on hysteresis based current control PWM named “Hi-PWM”, which has several advantages such as quick response of current, less fluctuation of switching frequency and less harmonic components.

Voltage, Current and Noise Harmonics

K. Kim, et al. [85], presented in this literature is proposed a new hybrid RPWM technique in order to disperse the acoustic switching noise spectra of an induction motor drive. The proposed RPWM pulses are produced through the logical comparison in this literature. It has been observed that total harmonic distortion in Indian Railway is 16.64%.

Multilevel Inverters

Rokan Ali, Ahmed S. Mekhilef, Hew Wooi Ping [11] explain new topology for symmetrical and asymmetrical multilevel inverter is introduced. Both types have many steps with fewer power electronic switches, which results in reduction of installation area and cost and have simplicity of control system. José Rodríguez, Jih-Sheng Lai and Fang Zheng Peng [12] presents the most important topologies like diode-clamped inverter (neutral-point clamped), capacitor-clamped (flying capacitor), and cascaded multicell with separate dc sources. Emerging topologies like asymmetric hybrid cells and soft-switched multilevel inverters are also discussed. This paper also presents the most relevant control and modulation methods developed for this family of converters: multilevel sinusoidal pulse width modulation, multilevel selective harmonic elimination, and space-vector modulation. Amit Kumar Gupta, and Ashwin M. Khambadkone [13], proposes a simple space vector pulse width modulation algorithm for a multilevel inverter for operation in the over modulation range. The proposed scheme easily determines the location of the reference vector and calculates on-times. Longhua Zhou, Qing Fu, Xiangfeng Li and Changshu Liu [14] proposes a novel Multilevel Power Quality Compensator (MPQC).

This novel MPQC is composed of two single-phase cascaded inverters by sharing the DC capacitors each cascaded Inverter is made of two cascaded H-bridge inverters and the ratio of the DC voltage is 3:1, then, connects to traction power system via grid-transformer. R. W. Menzies, P. Steimer, and J. K. Steinke [15], investigates the use of a five-level GTO voltage-sourced inverter for large induction motor drives, The advantages of such a drive are that single GTO thyristors may be used at each level, thereby avoiding the need for series connection of the thyristors. The thyristors are well protected from over voltages by the clamping action of the dc supply capacitors. Hyo L. Liu, Gyu H. Cho, and Sun S. Park [16] done the comparative studies between harmonic elimination and optimal PWM strategies are given for high power three level inverter feeding induction motor. An effective PWM map construction method based. Jie Zhang [17]

presents a high performance control of a cage induction motor drive fed by a 100 Hp three-level IGBT inverter operating at a low switching frequency. J. Shen and N. Butterworth [18] analyses the merits and demerits of three-level PWM converters through the comparison with two-level PWM converters. A general method for analyzing the switching modes of PWM converters is described and an analysis of the three-level PWM converter is presented as an example. Wensheng Song, Xiaoyun Feng, and Keyue Smedley [19] proposes a control and modulation scheme for the single-phase three-level NPC converter. Firstly, an active and reactive current decoupled control scheme in d-q synchronous frame is presented for single-phase three-level NPC converter to reduce the influence between the traction power supply fluctuating voltage and the traction drive system. Secondly, a new space vector PWM (SVPWM) scheme is provided to restrict the voltage step of the input port voltage within half of DC-link voltage. Shutian Zhang, Lin Wu, Congwei Liu, Longcheng Tan, Qiongquan Gel [20] presents a three-level neutral point clamped (NPC) back-to-back converter with IGCT for high power ac drive. The power circuit topology of the three-level NPC back-to-back converter and the hardware control system based VMEBUS and TMS320F28335 DSP are introduced.

Urmila BANDARU, Subba D RAYUDU [21] presents a comparative study of orientation of higher ordered harmonics with increase in switching frequency around the frequency modulation index of nine level diode clamped inverter for different Switching frequency Multicarrier Pulse width Modulation. Juan W. Dixon, Micah E. Ortúzar Luis A. Morán explain [22] the converter, with their 81 levels of voltage, can generate an excellent voltage waveform. The advantages and drawbacks of this kind of converter have been discussed. Juan W. Dixon, Micah Ortúzar and Felipe Ríos [23] investigated T the main advantage of this kind of topology is that it can generate almost perfect current or voltage waveforms, because it is modulated by amplitude instead of pulse-width. That means that the pulsating torque generated by harmonics can be eliminated, and power losses into the machine due to harmonic currents can also be eliminated. Juan Dixon, Javier Pereda, Carlos Castill and Sebastián Bosch [24] focused on a 27-level asymmetric inverter, but the strategy, using only one power supply, can be applied to converters with any number of levels.

Summary of the Paper

The following tables give summary of the paper as:

Table 1: Reduction of Harmonics Point of View

Parameter	Total No. of Literatures Review Out of 45 Literatures	% of Literature Reviews Out of 45 Literatures
Voltage harmonics	09	20
Current harmonics	08	17.77
Voltage and current harmonics	12	26.67
Harmonic distortion factor	10	22.22
Multilevel inverters	14	31.11

Reduction of Harmonics by Various Techniques

From above tables 1, it is concluded that the 20% of total literatures are reviews based on Voltage Harmonics, 17.77% of total literatures are reviews based on Current Harmonics, 26.67% of total literatures are reviews on based Voltage & Current Harmonics, 22.22% of total literatures are reviews on based Harmonics Distortion Factor (HDF), 31.11% of total literatures are reviews on based multilevel inverter. Finally it is concluded that the maximum research work carryout on multilevel inverters.

No. of Switches, No. of Levels, Space Vector Method and Other Methods in Multilevel Inverter**Table 2: Different Methods in Multilevel Inverters**

Parameter	Total No. of Literatures Review Out of 34 Literatures	% of Literature Reviews Out of 34 Literatures
No of level	12	35.29
No. of switches	8	23.53
Other methods	10	29.41

From above table no 2, it is concluded that the 35.29% of total literatures reviews based on no. of level used in multilevel inverters (2-level to 81- level).based on no. of switches is 23.53%. Other methods like space vector method, capacitor charging method, wavelet transform method is 29.41%.

CONCLUSIONS

This paper has been addressed a survey of several technical literature concerned with total harmonic distortion and multilevel inverter. There are various methods for reducing the THD. But among all implementation of multilevel inverter method will be more effective. A literature survey also show that the achieve significant improvements in operating parameters of the multilevel such as reduction harmonics such as voltage, current harmonics, power factor, switching frequency, and others parameters. Authors strongly believe that this survey article will be very much useful to the researchers for finding out the relevant references as well as the previous work done in the field of reduction of harmonic and implementation of multilevel inverter for reduction of harmonic loss. So that further research work can be carried out. Even through, excellent advancements have been made in classical method i.e. harmonics distortion factor they suffer with the following disadvantages: In most cases, mathematical formulations have to be simplified to get the solutions because of the extremely limited capability to solve real-world large-scale multilevel inverter.

REFERENCES

1. N.Gunavardhini¹, M.Chandrasekaran² A. D.Thirumoorthy, "A Study on Harmonics in Indian Railway Traction." IOSR Journal of Electrical and Electronics Engineering (IOSRJEET) ISSN: 2278-1676 Volume 2, Issue 1 (July-Aug. 2012), PP 01-04
2. Shu-Guang Sun, Jing-Qin Wang, Shun-Quan Shi. Study of Two Detection Methods for Harmonics and Reactive Currents. Seventh International Conference on Machine Learning and Cybernetics, Kunming, 12-15 July 2008
3. Yu Han, Cui Zhengpai, Li Sheng, Liu Qihui, Long Yunbo, Zhang Jianhua. Approach on Detection of Reactive and Harmonic Currents in Single-phase Circuit. 2006 IEEE
4. H. J. Chuang, , C. S. Chen, C. H. Lin, and H. M. Shiao Stochastic Harmonic Load Flow Analysis and Distortion Mitigation of Mass Rapid Transit Systems. June 23 2003 IEEE Bolona ITALY.
5. I. Zamora¹, P. Eguia, A. J. Mazón, E. Torres, K. J. Sagastabeitia. Using Active Filters to Reduce THD in Traction Systems.
6. Karel Hlava, Radovan Doleček. Sine Wave Distortion Of The Voltage for Contact Line System OF 25 KV, 50 hz at Czech Railways. Scientific Papers of the university of Pardubice. October (2004)

7. Adrian David Cheok Shoichi Kawamoto, Takeo Matsumoto, and Hideo Obi. High Power AC/DC Converter and DC/AC Inverter for High Speed Train Applications. 2000 IEEE pp423-429
8. Vasanthi V, and Ashok S, Harmonic Issues in Electric Traction System. 2011 IEEE
9. Urmila Bandaru¹, Subba D Rayudu¹. Harmonic Orientation of Pulse Width Modulation Technique in Multilevel Inverters Power Engineering and Electrical Engineering. Volume: 9 | Number: 1 | 2011
10. Shouji Onda, Katsumi Maekawa. Hardware Embedded Current Control PWM “Hi-PWM”. The 2010 International Power Electronics Conference 2010 IEEE pp 1596-1599
11. Rokan Ali Ahmed S. Mekhilef Hew Wooi Ping. New multilevel inverter topology with reduced number of switches. 14th International Middle East Power Systems Conference (MEPCON’10), Cairo University, Egypt, December 19-21, 2010, pp 565-570.
12. José Rodriguez, Jih-Sheng Lai, and Fang Zheng Peng. Multilevel Inverters: A Survey of Topologies, Controls, and Applications. IEEE Transactions on Industrial ELECTRONICS, VOL. 49, NO. 4, August 2002 pp 724-739.
13. Amit Kumar Gupta, and Ashwin M. Khambadkone, A General Space Vector PWM Algorithm for Multilevel Inverters, Including Operation in Over modulation Range. IEEE Transactions on Power Electronics, Vol. 22, NO. 2, MARCH 2007pp 517-527
14. Longhua Zhou¹, Qing Fu¹, Xiangfeng Li and Changshu Liu A Novel Multilevel Power Quality Compensator for Electrified Railway 2009 IEEE
15. R. W. Menzies, P. Steimer, and J. K. Steinke. Five-Level GTO Inverters for Large Induction Motor Drives. IEEE Transactions ON Industry Applications, VOL. 30, NO. 4, JULY / AUGUST 1994 pp 938-942.
16. Hyo L. Liu, Gyu H. Cho, and Sun S. Park. Optimal PWM Design for High Power Three-Level Inverter through Comparative Studies. IEEE Transactions on Power Electronics, VOL. 10, NO. 1, JANUARY 1995. pp38-48.
17. Jie Zhang. High Performance Control of A Three-level IGBT inverter fed AC Drive. 1995 IEEE pp 21-28.
18. J. Shen N. Butterworth Analysis and design of a three-level PWM converter system for railway-traction applications. IEEE ProcElectr. Power App, Vol. 144, No. 5, September 1997 pp 357-362
19. Wensheng Song, Xiaoyun Feng, and Keyue Smedley². A Space-Vector PWM Method for Single-Phase Three-level Neutral-Point Clamped Converter. 2011 IEEE pp 521-528.
20. Shutian Zhang, Lin Wu, Congwei Liu¹, Longcheng Tan¹, Qiongxuan Ge¹. Three-Level NPC Back-to-Back Converter with IGCT for High Power AC Drive
21. Urmila Bandaru, Subba D Rayudu Harmonic orientation of Pulse Width Modulation technique in Multilevel Inverters. Advances in Electrical and Electronic Engineering. Volume: 9 | Number: 1 | 2011 | March. pp29-35
22. Juan W. Dixon, Micah E. Ortúzar Luis A. Moran Drive System for Traction Applications Using 81-Level Converter.
23. Juan W. Dixon, Micah Ortúzar and Felipe Ríos Traction Drive System for Electric Vehicles, Using Multilevel Converters IEEE PP 188-198

24. Juan Dixon, Javier Pereda, Carlos Castillo, and Sebastián Bosch. Asymmetrical Multilevel Inverter for Traction Drives Using Only One DC Supply. IEEE Transactions on Vehicular Technology, VOL. 59, NO. 8, October 2010 PP 3736-3744.
25. L.M'Tolbert, F.Z.Peng, Multilevel Inverter For Large Automotive Drive. Second International Conference June 1997, vol 2, pp 209-214.
26. von Jouanne, A.; Dai, S.; Zhang, H.; „A multilevel inverter approach providing DC-link balancing, ride-through enhancement, and common-mode voltage elimination”, Industrial Electronics, IEEE Transactions on, Volume 49, Issue 4, Aug. 2002 Page(s):739 – 745
27. Schibli N. P., Nguyen T., and Rufer A. C.; “A Three-Phase Multilevel Converter for High- Power Induction Motors”, IEEE transactions on Power Electronics, VOL. 13, NO. 5, September 1998, pp. 978-986
28. Corzine, K.A.; Baker, J.R.; “Multilevel voltage-source duty-cycle modulation: analysis and Implementation”, IEEE Transactions on Industrial Electronics, Volume 49, Issue 5, Oct. 2002 Page(s):1009 – 1016
29. Bueno, E.J.; Garcia, R.; Marron, M.; Urena, J.; Espinosa, F.; “Modulation techniques comparison for three levels VSI converters”, IECON 02 [Annual Conference of the Industrial Electronics Society, IEEE 2002 28th], volume 2, 5-8 Nov. 2002 Page(s):908 – 913
30. Gopakumar, K.Tekwani, P.N.Kanchan, R.S.;A “Dual Five-Level Inverter-Fed Induction Motor Drive With Common-Mode Voltage Elimination and DC-Link Capacitor Voltage Balancing Using Only the Switching-State Redundancy—Part 1 Transactions on Industrial Electronics, IEEE, Volume 54, Issue 5, Oct. 2007 Pages: 2600 – 2608
31. Gopakumar, K.; Tekwani, P.N.Kanchan, R.S. “A Dual Five-Level Inverter-Fed Induction Motor Drive With Common-Mode Voltage Elimination and DC-Link Capacitor Voltage Balancing Using Only the Switching-State Redundancy—Part II”, Transactions on Industrial Electronics, IEEE, Volume 54, Issue 5, Oct. 2007 Page(s): 2609 – 2617
32. Helle, L. Munk-Nielsen, S. Enjeti, P.Generalized discontinuous DC-link balancing modulation strategy for three-level inverters”, Power Conversion Conference, 2002. PCC Osaka 2002. Proceedings of the, Volume 2, 2-5 April 2002 Page(s):359 - 366 vol.2.
33. Krug D., Bernet S., Fazel S. S., Jalili K. and Malinowski M., “Comparison of 2.3-kV Medium- Voltage Multilevel Converters for Industrial Medium-Voltage Drives”, IEEE Transaction on industrial Electronics, Vol. 54, No. 6, December 2007, pp.2979-2992
34. Loh, P.C. Pang, G.H.H. Holmes, D.G. “Multi-level discontinuous pulse width modulation: common mode voltage minimization analysis”, Electric Power Applications, IEE Proceedings -Volume 151, Issue 4, 7 July 2004 Page(s):477 – 488
35. Malinowski M.; Stynski, S. “Simulation of Single-phase Cascade Multilevel PWM Converters” EUROCON 2007, 9-12th Sep. Warsaw, Poland, on CD.
36. McGrath, B.P.; Holmes, D.G.; Maynard, T.; “Reduced PWM harmonic distortion for multilevel inverters operating over a wide modulation range”, IEEE Transactions on Power Electronics, Volume 21, Issue 4, July 2006 Page(s): 941 – 949

37. Marchesoni, M.Tenca, P. "Diode-clamped multilevel converters: a practicable way to balance DC-link voltages", *Industrial Electronics, IEEE Transactions on*, Volume 49, Issue 4, Aug. 2002 Page(s):752 – 765
38. Schibli N. P., Nguyen T., and Rufer A. C.; "A Three-Phase Multilevel Converter for High-Power Induction Motors", *IEEE transactions on Power Electronics*, VOL. 13, NO. 5, September 1998, pp. 978-986
39. Zhiguo Pan; Fang Zheng Peng; Corzine, K.A.; Stefanovic, V.R.; Leuthen, J.M.; Gataric, S.; "Voltage balancing control of diode-clamped multilevel rectifier/inverter systems", *IEEE Transactions on Industry Applications*, Volume 41, Issue 6, Nov.-Dec. 2005 Pages:1698 –1706
40. J. Rodríguez, J.S. Lai, F. Z. Peng, "Multilevel inverters: A survey of topologies, controls, and applications," *IEEE Trans. On Ind. Electron*, vol. 49, no. 4, pp. 724–738, Aug. 2002.
41. J.S. Lai, F.Z. Peng, "Multilevel converters— A new breed of power converters," *IEEE Trans. On Ind. Appl.*, vol. 32, pp. 509–517, May– June 1996.
42. L.M. Tolbert, F.Z. Peng, T.G. Habetler, "Multilevel converters for large electric drives," *IEEE Trans. On Ind. Appl.*, vol. 35, pp. 36–44, Jan.–Feb. 1999
43. R.H. Baker, L.H. Bannister, "Electric power converter," U.S. Patent 3867643, Feb. 1975.
44. L.M. Tolbert, F.Z. Peng, T.G. Habetler, "Multilevel inverters for electric vehicle applications," in *Conf. Proc. IEEE Workshop on Power Electron., in Transportation*, Dearborn, Michigan, pp. 1424– 1431, 22–23 Oct. 1998
45. E. Cengelci, S.U. Sulistijo, B.O. Woom, P. Enjeti, R. Teodorescu, F. Blaabjerg, "A new medium voltage PWM inverter topology for adjustable speed drives," in *Conf. Rec. IEEE Ind. Appl. Society Annu. Meeting*, St. Louis, MO, pp. 1416–1423, Oct. 1998
46. R.W. Menzies, Y. Zhuang, "Advanced static compensation using a multilevel GTO thyristor inverter," *IEEE Trans. On Power Delivery*, vol. 10, no. 2, pp. 732–738, Apr. 1995.
47. F.Z. Peng, J.S. Lai, J.W. McKeever, J. VanCoevering, "A multilevel voltage-source inverter with separate dc sources for static var generation," *IEEE Trans. On Ind. Electron.*, vol. 32, no. 5, pp. 1130– 1138, Sept. 1996.
48. F.Z. Peng, J.S. Lai, "Dynamic performance and control of a static var generator using cascade multilevel inverters," *IEEE Trans. On Ind. Electron*, vol. 33, no. 3, pp. 748–755, May 1997.
49. F.Z. Peng, J.W. McKeever, D.J. Adams, "A power line conditioner using cascade multilevel inverters for distribution systems," in *Conf. Rec. IEEE Ind. Appl. Society 32nd Annu. Meeting*, pp. 1316–1321, 1997.
50. L.M. Tolbert, F.Z. Peng, "Multilevel converters as a utility interface for renewable energy systems," in *Rec., IEEE Power Engineering Society Summer Meeting*, pp. 1271–1274, 2000
51. J. N. Chiasson, L. M. Tolbert, K. McKenzie, Z. Du, "Harmonic Elimination in Multilevel Converters," *IASTED International Conference on Power and Energy Systems (PES 2003)*, February 24-26, 2003, Palm Springs, California, pp. 284-289.
52. J. S. Lai, F. Z. Peng, "Multilevel Converters - A New Breed of Power Converters," *IEEE Transactions on Industry Applications*, vol. 32, no. 3, May 1996, pp. 509-517.
53. F. Z. Peng, J. W. McKeever, D. J. Adams, "A Power Line Conditioner Using Cascade Multilevel Inverters for Distribution Systems," *IEEE Transactions on Industry Applications*, vol. 34, no. 6, Nov. 1998, pp. 1293-1298.

54. L. M. Tolbert, F. Z. Peng, T. G. Habetler, "A Multilevel Converter-Based Universal Power Conditioner," IEEE Transactions on Industry Applications, vol. 36, no. 2, Mar./Apr. 2000, pp. 596-603
55. L. M. Tolbert, J. N. Chiasson, K. McKenzie, Z. Du, "Elimination of Harmonics in a Multilevel Converter for HEV Applications," The 7th IEEE Workshop on Power Electronics in Transportation, October 24-25, 2002, Auburn Hills, Michigan, pp. 135-142.
56. J. N. Chiasson, L. M. Tolbert, K. McKenzie, Z. Du, "Eliminating Harmonics in a Multilevel Converter using Resultant Theory," IEEE Power Electronics Specialists Conference, June 23-27, 2002, Cairns, Australia, pp. 503-508.
57. J. N. Chiasson, L. M. Tolbert, K. J. McKenzie, Z. Du, "A New Approach to the Elimination of Harmonics in a Multilevel Converter," 10th European Conference on Power Electronics and Applications - EPE 2003, September 2-4, 2003, Toulouse, France
58. Martin Veenstra, Investigation And Control Of A Hybrid Asymmetric Multi-Level Inverter For Medium-Voltage Applications, 2003, Lausanne, EPFL
59. N.A. Rahim (Member IEEE), E.A.Mahrous, K.M.Sor(Senior Member IEEE), "Modeling And Simulation of Linear Generator PWM Multilevel Inverter", National Power and Energy Conference (PE Con) 2003 Proceedings, Malaysia.
60. G. Sinha, T.A. Lipo, "A Four Level Rectifier Inverter System for Drive Applications", IEEE Annual Meeting 1996, pp 980-987
61. G.Carrara, D.Casini, S.Gardella, R.Salutari, "Optimal PWM for the Control of Multilevel Voltage Source Inverter", Fifth Annual European Conference on Power Electronics, volume 4, 1993, pp 255-259
62. Samir Kouro, Mariusz Malinowski et. al., "Recent Advances and Industrial Applications of Multilevel Converters", IEEE Transactions on industrial electronics, vol.57, no.8, pp. 2553-2580, Aug 2010
63. Farhad Shahnia and B. B. Sharifian, "Harmonic analysis and modelling of transformerless electric railway traction drives," 13th International conference on Electrical Drives and Power Electronics (EDPE), Dubrovnik, Croatia, 26-28 Sep 2005.
64. Leopoldo G. Franquelo, Jose Rodriguez, et. al., "The Age of Multilevel Converters arrives", IEEE Industrial Electronics Magazine, vol. 2, Issue 2, pp. 28-39, June 2008
65. V. Kumar Chinnaiyan, Dr. Jovitha Jerome, J. Karpagam, and T. Suresh, "Control techniques for Multilevel Voltage Source Inverters," in Proceedings of The 8th International Power Engineering Conference (IPEC 2007), Singapore, pp. 1023-1028, 3-6 Dec 2007.
66. R. J. Hill, "Traction Drives and Converters", 2nd IEE Residential Course on Railway Electrification Infrastructure Systems, IEE Digest, vol. 2005, Issue 1087, Canterbury, UK, 23-27 May 2005
67. R. J. Hill, "Electric railway traction Part 2 Traction drives with three-phase induction motors", Power Engineering Journal, pp. 143-152, Jun 1994
68. Jin Wang and Damoun Ahmadi, "A Precise and Practical Harmonic Elimination Method for Multilevel Inverters", IEEE Transactions on Industry Applications, vol. 46, no. 2, pp. 857-865, Mar-Apr 2010

69. S. H. Hosseini, M. Ahmadi, S. Ghassem Zadeh, "Reducing the output harmonics of Cascaded H-bridge Multilevel Inverter for Electric Vehicle Applications", 8th International Conference on Electrical Engineering/ Electronics, Computer Telecommunications and Information Technology (ECTI-CON 2011), Thailand, pp. 752-755, 17-19 May 2011
70. V. Naga Bhaskar Reddy, V. Narasimhulu, Dr. Ch. Sai Babu, "Control of Cascaded Multilevel Inverter by using carrier based PWM technique and implemented to Induction Motor drive," International Journal on Automatic Control and System Engineering (ICGST-ACSE Journal), vol. 10, Issue 1, Dec 2010.
71. Wenyi Zhang, Qiang Zhang, Wensheng Chen and Liuzhong Zhang, "Analyzing of Voltage Source Selective Harmonic Elimination Inverter," in Proceedings of the 2011 IEEE 74 International Conference on Mechatronics and Automation, Beijing, China, pp. 1888-1892, 7-10 Aug 2011.
72. F. Z. Peng, J. W. McKeever and D. J. Adams, "Cascade Multilevel Inverters for Utility Applications", in Proceedings of Industrial Electronics Conference (IECON), vol. 2, pp. 437-442, 1997
73. R. Lund, M. D. Manjrekar, P. Steimer, T. A. Lipo, "Control strategies for a hybrid seven-level inverter", in Proceedings of the European Power Electronic Conference, Lausanne, Switzerland, Sep 2009
74. Toshiji Kato, "Sequential Homotopy-Based Computation of Multiple Solutions for selected Harmonic Elimination in PWM Inverter", IEEE Transaction on Circuits and Systems-I: Fundamental Theory and Applications, vol., no. 5, pp. 586-593, May 1999.
75. Burak Ozpineci, Leon M. Tolbert, John N. Chiasson, "Harmonic Optimisation of Multilevel Converters using Genetic Algorithms", IEEE Power Electronics Letters, vol. 3, no. 3, pp. 92-95, Sep 2005.
76. Jagdish Kumar, Biswarup Das, and Pramod Agarwal, "Selective Harmonic Elimination technique for a Multilevel inverter," in Proc. of 15th National Power Systems Conference (NPSC), IIT Bombay, pp. 608-613, 16-18 Dec 2008.
77. http://en.wikipedia.org/wiki/Railway_electric_traction
78. Mauro Carpitia, Mario Marchesoni, Marc Pellerin, and David Moser, "Multilevel Converter for Traction Application: Small Scale Prototype tests Result", IEEE Transaction on Industrial Electronics, vol. 55, no. 5, pp. 2203-2212, May 2008.
79. H. D. Awasty, "Railway Electrification in India", in Proceedings of IEE, vol III, no. 12, pp. 2071-2074, May 2008
80. www.railway_technical.com
81. K. Thiagarajah, V. T. Ranganathan, B. S. Ramakrishna Iyengar, "A high switching frequency IGBT PWM rectifier / inverter system for AC motor drives operating from single phase supply", IEEE Transactions on Power Electronics, vol. 6, no. 4, pp. 576-584, Oct. 1991.
82. A.K.Verma, P.R.Thakur, K.C.Jana, and G.Buja, "Cascaded multilevel inverter for Hybrid electric vehicles," 2010 India International Conference on Power Electronics (IICPE), New Delhi, 28-30 Jan 2011.

83. Adrian David Cheok, Shoichi Kawamto, Takeo Matsumoto and Hideo Obi, “ High power AC/DC converter and DC/AC inverter for high speed train applications”, in Proceedings of IEEE TECON 2000, vol. 1, pp. 423-428, 24-27 Sep 2000
84. J. S. Lai and F. Z. Peng, “Multi level converters -a new breed of power converters,” IEEE Trans. Ind. Applicant., vol.32,pp. 509-517, May/June 1996
85. K. Kim, Y. Jung, and Y. Lim, “A New Hybrid Random PWM Scheme,” IEEE Trans. On Power Electronics, vol. 24, No. 1, pp. 192-200, Jan 2009.
86. Rashid, M.H., ‘Power Electronics – Circuits Device and Applications
87. Singn. M.D and Kanchandani-‘Power electronics’.

